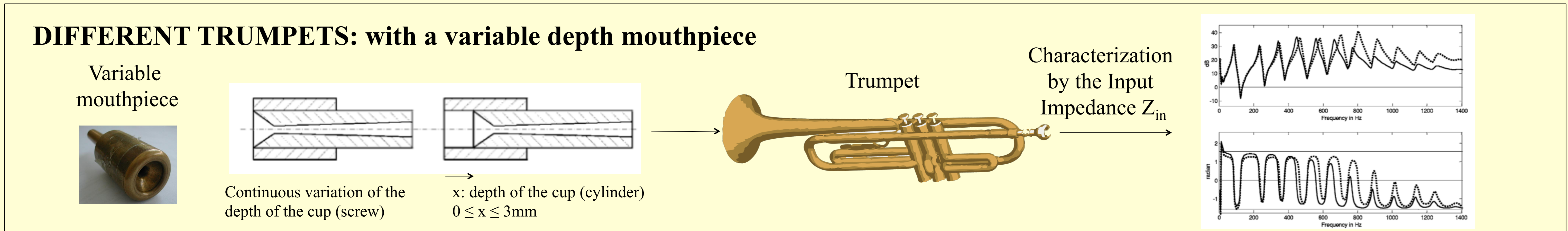


INHARMONICITY OF A TRUMPET WITH A VARIABLE DEPTH MOUTHPIECE

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3 INVESTIGATION METHODS:

Resonance frequencies of the INPUT IMPEDANCE

- Measurement of the input impedance Z_{in} for one given depth ($x=0$).
- Extrapolation of the input impedance for different depths by impedance calculation (addition of a cylinder of length x with the transmission line formalism)
- Extraction of the resonances frequencies of the impedance, for different mouthpiece depths

Playing frequencies of SIMULATED SOUNDS

- Simulation in the frequency domain with the harmonic balance technique:

$$p(t) = C_o + \sum_{n=1}^N A_n \cdot \cos(2\pi n F_o t + \varphi_n)$$

Virtual musician embouchure

Input impedance Z_{in}

Simulations

P_m : pressure in the mouth
 f_l : resonance frequency of the lips
 m_l : mass of the lips

Amplitude of the harmonics: A_1, \dots, A_6
 Playing frequency: F_0

- 4 Fingerings: D₀ D₁ D₂ D₂₃
- 5 Regimes: r2 to r6
- 30 Mouthpiece positions:
- 300 virtual “embouchures”

Playing frequency of a note averaged on the different embouchures

Playing frequencies of RECORDED SOUNDS

- Trumpet with the variable mouthpiece played by a musician
- Extraction of the playing frequencies of the sounds

- 4 Fingerings: D₀ D₁ D₂ D₂₃
- 5 Regimes: r2 to r6
- 3 Mouthpiece positions: 0mm, 1.5mm and 3mm
- 3 repetitions

Playing frequency of a note averaged on the 3 repetitions

OBJECTIVE:

Study of the agreement between the playing frequencies of the recorded sounds, the playing frequencies of the simulated sounds, the resonance frequencies of the impedance

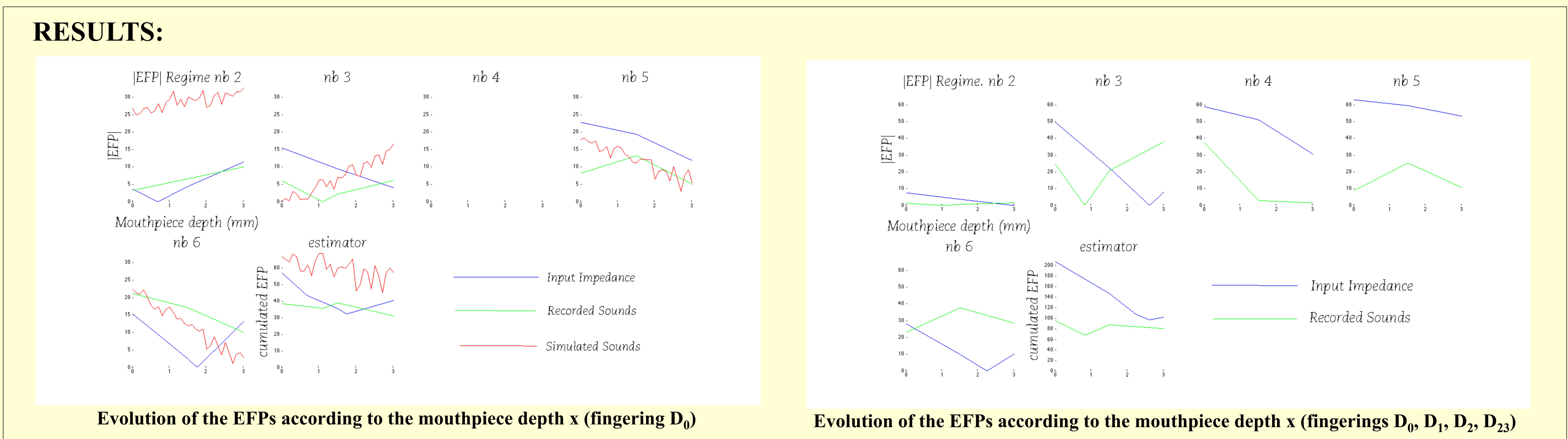
=> Prediction of the intonation

ESTIMATION OF THE INHARMONICITY: The Equivalent Fundamental Pitch (EFP)

- Choice of a reference $f(ref)$: 4th regime of the fingering D₀ (tuning note)
- EFP of each note (cent):

$$EFP(i) = 1200 \log_2 \left(\frac{f(i)/i}{f(ref)/ref} \right)$$

- Proposition of a estimator of the global intonation of the whole trumpet

$$Intonation_{estim} = \sum_{j \in \{fingerings\}} \sum_{i \in \{regimes\}} |EFP_{ij}|$$


CONCLUDING REMARKS

- For Fingering D₀: noticeable similarities in the global behaviour for the 3 methods:
 - The general evolution trends of the EFPs for the different regimes are consistent (except for regime 3 for the impedance)
 - The absolute values of the EFPs are consistent (except for regime 2 and the simulations)
 - Influence of the virtual embouchure on the simulated sounds
- For all the fingerings
 - The precision of the intonation predictions remains low: not reasonable to make accurate predictions of the intonation from the impedance. Results in progress for the simulations...